High Resolution Photoexcitation Measurements Exacerbate the Long-Standing Fe XVII Oscillator Strength Problem

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For more than 40 years, most astrophysical observations and laboratory studies of two key soft x-ray diagnostic $2p \rightarrow 3d$ transitions, $3C$ and $3D$, in Fe XVII ions found oscillator strength ratios $f(3C)/f(3D)$ disagreeing with theory, but uncertainties had precluded definitive statements on this much studied conundrum. Here, we resonantly excite these lines using synchrotron radiation at PETRA III, and reach, at a millionfold lower photon intensities, a 10 times higher spectral resolution, and 3 times smaller uncertainty than earlier work. Our final result of $f(3C)/f(3D) = 3.09(8)(6)$ supports many of the earlier clean astrophysical and laboratory observations, while departing by five sigmas from our own newest large-scale ab initio calculations, and excluding all proposed explanations, including those invoking nonlinear effects and population transfers.

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conditions, velocity turbulences, and opacities [5–15]. However, for the past four decades, their observed intensity ratios persistently disagree with advanced plasma models, diminishing the utility of high resolution x-ray observations. Several experiments using electron beam ion trap (EBIT) and tokamak devices have scrutinized plausible astrophysical and plasma physics explanations as well as the underlying atomic theory [16–23], but also revealed clear departures from predictions while broadly agreeing with astrophysical observations [19,20,24]. This has fueled a long-lasting controversy on the cause being a lack of understanding of astrophysical plasmas, or inaccurate atomic data.

A direct probe of these lines using an EBIT at the Linac Coherent Light Source (LCLS) x-ray free-electron laser (XFEL) found again their oscillator strength ratio \( f(3C)/f(3D) \) to be lower than predicted, but close to astrophysical observations [25]. This highlighted difficulties with oscillator strength calculations in many-electron systems [24–31]. Nonetheless, at the high peak brilliance of the LCLS XFEL, nonlinear excitation dynamics [32,33] or nonequilibrium time evolution [34] might have affected the result of Bernitt et al. [25]. An effect of resonance-induced population transfer between Fe XVI and Fe XVII ions was also postulated [35] since the Fe XVI line \( C(3s3d_{5/2}^{1/2}) \rightarrow (2p^63s)_{J=1/2} \) appeared blended with the Fe XVII line \( 3D \). A recent semiempirical calculation [36] reproduces the LCLS results [25] by fine-tuning relativistic couplings and orbital relaxation effects, but its validity has been disproved [37].

In this Letter, we report on new measurements of resonantly excited Fe XVI and Fe XVII with a synchrotron source at tenfold improved spectral resolution and millionfold lower peak photon flux than in [25], suppressing nonlinear dynamical effects [32,34,38] and undesired ion population transfers [35]. We also carry out improved large-scale calculations using three different advanced approaches [39–41], all showing a five-sigma departure from our experimental results.

We used the compact PolarX-EBIT [42], in which a monoenergetic electron beam emitted by an off-axis cathode (see Fig. 1) is compressed by a magnetic field. At the trap center, it collides with a beam of iron-pentacarbonyl molecules, dissociating them, and producing highly charged Fe ions with a relative abundance of Fe XVI to Fe XVII close to unity. These ions stay radially confined by the negative space charge of the \( \sim 2 \)-mA, 1610-eV (\( \approx 3 \) times the Fe XVI ionization potential) electron beam and axially by potentials applied to surrounding electrodes.

Monochromatic, circularly polarized photons from the P04 beamline [43] at the PETRA III synchrotron photon source enter through the electron gun, irradiate the trapped ions, and exit through the collector aperture. They can resonantly excite x-ray transitions on top of the strong electron-induced background due to ionization, recombination, and excitation processes. A side-on-mounted energy-resolving windowless silicon drift photon detector (SDD) equipped with a 500-nm thin aluminum filter registers these emissions.

By scanning the P04 monochromator between 810 and 830 eV, we excite the Fe XVII lines 3C and 3D, as well as the Fe XVI lines \( B((2p^5)_{1/2}(3s3d_{3/2})_{j=1/2}) \rightarrow (2p^63s)_{j=1/2} \) and \( C \). They are also nonresonantly excited by electron impact as the electron beam energy is well...
above threshold [21,23]. This leads to a strong, nearly constant x-ray background at the same energies as the photoexcited transitions but independent of the exciting photon-beam energy. In our earlier work [25], we rejected this background by detecting the fluorescence in time coincidence with the sub-picosecond-long LCLS pulses of $\approx10^{11}$ photons each at 120/s. Because of much longer and weaker 50-ps-long pulses ($\approx10^3$ photons, $6 \times 10^5$/s repetition rate) at P04 and the limited time resolution of SDD, we could not use the coincidence method and reached a signal-to-background ratio of only $\sim5\%$. To improve this, we used a shutter to cyclically turn on and off the P04 photon beam.

Using a 50-$\mu$m slit width, we reached a resolving power of $E/\Delta E \approx 10000$, 10–15 times higher than that of Chandra and XMM-Newton grating spectrometers [44,45], and tenfold that of our previous experiment [25] (see the Supplemental Material [46]). We find a separation of 3C from 3D of $\Delta E_{3C-3D} = 13.398(1)$ eV and resolve for the first time the Fe XVII 3D line from the Fe XVI C one at $\Delta E_{3D-C} = 154.3(1.3)$ meV. This gives us the 3C/3D intensity ratio without having to infer a contribution of Fe XVI line C (in [25] still unresolved) from the intensity of the well-resolved Fe XVI A line. Thereby, we largely reduce systematic uncertainties and exclude the resonance-induced population transfer mechanism [35] that may have affected the LCLS result [25].

We apply three different methods (Fig. 1) to systematically measure the 3C/3D oscillator strength ratio. In method 1, we did not operate the photon shutter; instead, we repeatedly scanned the lines C and 3D (812.0–812.5 eV), as well as 3C (825.5–826.0 eV), in both cases using scans of 100 steps with 20-s exposure each (see Fig. 2). The SDD fluorescence signal was integrated over a 50-eV wide photon-energy region of interest (ROI) comprising 3C, 3D, and C and recorded while scanning the incident photon energy. By fitting Gaussians to the scan result, we obtain line positions, widths, and yields, modeling the electron-impact background as a smooth linear function [23]. The ratio of 3C and 3D areas is then proportional to the oscillator strength ratio [33]. However, given the low 5% signal-to-background ratio and long measurement times, changes in the background cause systematic uncertainties. In method 2, we fixed the monochromator energy to the respective centroids of C, 3D, and 3C found with method 1 and cyclically opened and closed the shutter for equal periods of 20 s to determine the background. The background-corrected fluorescence yields at the line peaks were multiplied with the respective linewidths from method 1, to obtain the 3C/3D ratio. Still, slow monochromator shifts from the selected positions could affect the results. To address this, in method 3, we scanned across the FWHM of C, 3D, and 3C in 33 steps with on-off exposures of 20 s, which reduced the effect of possible monochromator shifts. After background subtraction, we fit Gaussians to the lines of interest fixing their widths to values from method 1.

All three methods share systematic uncertainties caused by energy-dependent filter transmission and detector efficiency ($\sim1\%$) and by the incident photon beam flux variation ($\sim2\%$). Additionally, for method 1, we estimate systematic uncertainties from background ($\sim1.2\%$) and ROI selection ($\sim2.7\%$). In method 2, possible monochromator shifts from (set) line centroids and widths taken from method 1 cause a systematic uncertainty of $\sim3.5\%$. Analogously, for method 3, we estimate a $\sim3\%$ uncertainty.
FIG. 3. Present experimental 3C/3D ratios compared with previous predictions and experiments. Red band: combined results of the three different methods. Blue crosses: predictions [29,31,32,35,36,54–57]. Note that the validity of theory [36] has been disputed [37]. Blue solid circles: present FAC, large-scale CI calculations using a very-large-scale configuration interaction (CI) method, correlating all ten electrons, including Breit and quantum electrodynamical [62] corrections. We implemented a message passing interface (MPI) version of the CI code from [39] to increase the number of configurations to over 230,000, saturating the computation in all possible numerical parameters. Basis sets of increasing size are used to check for convergence, with all orbitals up to 12sp17dfg included in the largest version (the contributions of n > 12sp orbitals are negligible). We start with all possible single and double excitations from the 2s2p6, 2s2p53p even and 2s2p53s, 2s2p53d, 2sp63p, 2s2p54d, 2s2p55d odd configurations, correlating eight electrons. We separately calculate triple excitations and fully correlate the 1s2 shell, and also included dominant quadruple ones, finding them negligible. The line strengths S and 3C/3D oscillator strength ratio after several computation stages are summarized in the Supplemental Material [46] to illustrate the small effect of all corrections. Theoretical uncertainties are estimated based on the variance of results from the smallest to largest runs, size of the various effects, and small variances in the basis set construction. We verified that the energies of all 18 states considered, counted from the ground state, agree with the National Institute for Standards and Technology [51] database well within the experimental uncertainty of 0.05%. The theoretical 3C/3D energy difference of 13.44 eV is in agreement with the experiment to 0.3%.

We also carried out entirely independent large-scale calculations using the multireference multiconfiguration Dirac-Hartree-Fock (MR-MCDHF) approach [40] with up to 1.2 million configurations. First, the 2s2p53s, 2s2p53d, and 2s2p53p J = 1 levels were used as reference states to generate the list of configuration state functions with single and double exchanges from all occupied orbitals up to 12spdfgghil Virtual orbitals were added in a layer-by-layer manner. Subsequently, the role of triple excitations was studied by the CI method. In a second step, the multireference list was extended to include all J = 1 odd parity states, generated from the Ne-like ground state by single and double electron exchanges. Monitoring the convergence of the results for the addition of layers of virtual orbitals, we arrive at an oscillator strength ratio of 3.55(5) and to a 3C/3D energy splitting of 13.44(5) eV. Another full-scale CI calculation with more than a million configurations was carried out in the particle-hole formalism using AMBiT [41], agreeing well with the other theoretical results. Full details of all calculations can be found in the Supplemental Material [46].

We emphasize that there are no other known quantum mechanical effects or numerical uncertainties to consider within the CI and MCDHF approaches. With modern experiments at ultrabright light sources should take possible nonlinear effects into account.

due to the use of linewidth constraints from method 1. The weighted average of all three methods is f(3C)/f(3D) = 3.09(8), see Fig. 3 (see the Supplemental Material [46] for individual ratio and uncertainties). Note that the circular polarization of the photon beam does not affect these results, since 3C and 3D (both ΔJ = 1) share the same angular emission characteristics [47–50].

Calculations using a density-matrix approach by Oreshkina et al. [32,33], and the time-dependent collisional-radiative model of Loch et al. [34], pointed to a possible nonlinear response of the excited upper state populations in [25], reducing the observed oscillator strength ratio [38], which would depend on photon pulse parameters, like intensity, duration, and spectral distribution. It has been estimated that peak intensities above 10^12 W/cm^2 would give rise to nonlinear effects [32,38]. Fluctuations of the self-amplified spontaneous emission process at LCLS can conceivably generate some pulses above that threshold. At P04, we estimate a peak intensity of ~10^5 W/cm^2, more than 6 orders of magnitude below that threshold (see the Supplemental Material [46]). This could explain why the 3C/3D ratio in Bernitt et al. [25] is in slight disagreement with the present result. Nonetheless, our experiment validates the main conclusion of that work with reduced uncertainty. Our work implies that future
computational facilities and MPI codes, we have shown that all other contributions are negligible at the level of the quoted theoretical uncertainties. The significant improvements in experimental and theoretical precision reported here have only further deepened this long-standing problem. This work on the possibly so far most intensively studied many-electron ion in experiment and theory, finally demonstrates convergence of the dedicated atomic calculations on all possible parameters, excluding an incomplete inclusion of the correlation effects as potential explanation of this puzzle.

Our result is the presently most accurate on the $3C/3D$ oscillator strength ratio. Its excellent resolution suggests promising direct determinations of the natural linewidth. They depend on the Einstein $A$ coefficients, hence, on the oscillator strengths [63]. Thus, future measurements of individual natural linewidths of $3C$ and $3D$ not only would test theory more stringently than their oscillator strength ratio does, but also deliver accurate oscillator strengths.

Moreover, $3C$ and $3D$ with their, among many transitions, strong absorption and emission rates can also dominate the Planck and Rosseland mean opacity of hot plasmas [64–66]. Therefore, an accurate determination of their oscillator strengths may help elucidating the iron opacity issue [12,14,67], if, e.g., Rosseland mean opacity models [68,69] were found to use predicted oscillator strengths also in departure from experiments. Our result exposes in simplest dipole-allowed transitions of Fe XVII a far greater issue, namely, the persistent problems in the best approximations in use, and calls for renewed efforts in further developing the theory of many-electron systems.

Shortcomings of low-precision atomic theory for $L$-shell ions had already emerged in the analysis of high resolution Chandra and XMM-Newton data [13,19,20,24,70]. Similar inconsistencies were recently found in the high resolution $K$-shell x-ray spectra of the Perseus cluster recorded with the Hitomi microcalorimeter [71,72]. Moreover, recent opacity measurements [12,14] have highlighted serious inconsistencies in the opacity models used to describe the interiors of stars, which have to rely on calculated oscillator strengths.

All this shows that the actual accuracy and reliability of the opacity and turbulence velocity diagnostics are still uncertain, and with them, the modeling of hot astrophysical and high-energy density plasmas. The upcoming x-ray observatory missions XRISM [73] and Athena [74] will require improved and quantitatively validated modeling tools for maximizing their scientific harvest. Thus, benchmarking atomic theory in the laboratory is vital. As for the long-standing Fe XVII oscillator strength problem, our results may be immediately used to semiempirically correct spectral models of astrophysical observations.

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