

Homework 3 – PHYS626

Reading Material:

5.6-electron spin and fine structure

5.7-hyperfine structure

5.8 to 5.10 – additional breadth material on hydrogen

6.5 – terms and adding momentum

6.6 – excitation, x-rays, autoionization

6.7-exotic 'hydrogen' systems

- 1) Give all the possible electron configurations with term assignments for three electrons, one in a $k=1$ ($l=0, s$) state, one in a $k=2$ ($l=1, p$) state and one in a $k=3$ ($l=2, d$) state.
- 2) How large is the internal magnetic field produced by the $1s$ electron in the H atom at the location of the proton that causes the splitting of the two hyperfine components observed in the $\lambda=21\text{cm}$ transition.
- 3) In the classical model, the electron is described by a rigid sphere with radius r , mass m , and charge $-e$ uniformly distributed. Use both the classical value of the radius ($r=1.4 \cdot 10^{-15}\text{m}$) and the experimental value $r=10^{-18}\text{m}$ in the following:
 - a. What is the velocity of a point on the equator of this sphere when the angular momentum is $\sqrt{3}\hbar/2$
 - b. What would be the rotational energy of this sphere be compared to its rest mass energy $E_0=m_e c^2$?
- 4) By what factor does the radius of the Bohr orbit increase if the hydrogen atom in its ground state is excited by:
 - a. 12.09 eV
 - b. 13.387eV
- 5) Show that within the Bohr model, the ratio $\mu_L/|L|$ of the orbital magnetic moment to the angular momentum is independent of the principle quantum number n .